[CONTRIBUTION FROM THE DEPARTMENT OF CHEMISTRY OF THE UNIVERSITY OF CINCINNATI]

# THE ETHYL ACETATE EQUILIBRIUM. II.<sup>1</sup>

BY R. C. CANTELO AND R. D. BILLINGER RECEIVED JULY 10, 1929 PUBLISHED MARCH 6, 1930

The ethyl acetate equilibrium is represented by the chemical equation  $C_2H_5OH + HAc \longrightarrow C_2H_5Ac + H_2O$ ; and the equilibrium constant for the system is given by  $K_a = a_3a_4/a_1a_2$  where  $a_1, a_2, \ldots$  are the activities of the ethyl alcohol, acetic acid, .... in the system. In the absence of salts,  $K_a$  for this system is considered to be equal to  $K_E$ , where  $K_E = C_3C_4/C_1C_2$ , and  $C_1, C_2, \ldots$  are the molar concentrations.

Poznanski<sup>2</sup> states that Guldberg and Waage's<sup>3</sup> as well as van't Hoff's<sup>4</sup> determinations of the equilibrium constant  $K_E$  as calculated from the data of Berthelot and de Saint Gilles for this equilibrium are inaccurate. He states that Schwab<sup>5</sup> found  $K_E$  to vary from 1.0 to 6.8. Poznanski found experimentally that if varying quantities of acid are added to a mixture of alcohol and water,  $K_E$  varies on both sides of the value 3.79, which he found when 1 mole of acid + 1 mole of alcohol was used as the initial system.

We have throughout our experiments kept the proportions of acid, alcohol and water constant, so that for our purpose, namely, to discover the effect of the addition of salts upon  $K_E$ , we are justified in writing  $K_a = K_E$  in the absence of salts. However, when salts are present,  $K_E$ is no longer equal to  $K_a$ .  $K_a$  is a true constant and is related to  $K_E$  by the expression  $K_a = K_E \Sigma f_{C_2H_4OH}$ , where f is the activity coefficient; f for a given species, in the presence of salts, is a function of the ionic strength of the electrolytes present.<sup>6</sup>

In a previous paper' we have reported the effects of the salts sodium chloride, sodium iodide and sodium thiocyanate upon the equilibrium constant,  $K_E$ , of the ethyl acetate equilibrium. The present communication contains the results which we have obtained by the use of the salts sodium bromide, sodium acetate and sodium nitrite. It includes also the results of our study of the reaction rate constants for this system in the presence of the six salts cited.

<sup>1</sup> This paper and a previous one published under the same title represent an abstract of the thesis submitted by R. D. Billinger to the Graduate School of the University of Cincinnati, in partial fulfilment of the requirements for the degree of Doctor of Philosophy.

<sup>2</sup> Poznanski, Roczniki Chem., 8, 377 (1928); C. A., 23, 1559 (1929).

- <sup>8</sup> Guldberg and Waage, J. prakt. Chem., 19, 69 (1879).
- <sup>4</sup> Van't Hoff, Ber., 10, 669 (1877).
- <sup>5</sup> Schwab, Rec. trav. chim., 2, 46 (1883).
- <sup>6</sup> Debye and McAuley, Physik. Z., 26, 22 (1925).
- <sup>7</sup> Cantelo and Billinger, THIS JOURNAL, 50, 3212 (1928).

The general procedure in measuring the values of  $K_E$  is given in our first paper. The results obtained with the new series of salts are given in Tables I, II and III; the results for the complete series are shown graphically in Fig. 1. The salt concentration given is the molar concentration in the initial mixture used. The proportions of ethyl alcohol, acetic acid and salt solution were the same as those reported in our previous paper. The temperature was  $78^{\circ}$ .

TABLE I

	Effe	CT OF SODIUM B	ROMIDE		
Salt concn.,	Sample	$K_E$	Av. K <sub>F</sub>	$\Sigma f$	
0	Α	3.686	9 705	1	
0	В	3.725	3.700		
0.096	А	4.059	1 068	0.01	
	В	4.077	4,000	0.91	
.191	Α	4.094	4 103	00	
	В	4.111	4.100	.90	
. 289	Α	4.254	4 956	87	
	в	4.257	4.200	.01	
.382	Α	4.461	4 480	. 83	
	В	4.499	1.100		

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	-	LABLE II	L			T	ABLE II	1	
Еı	FECT O	F SODIUN	и Асетат	E	E	FFECT C	F Sodiu	M NITRIT	E,
Conen.	Sample	$K_E$	Av. $K_E$	$\Sigma f$	Couten.	Sample	$K_E$	Av. $K_E$	$\Sigma f$
0.097	Α	3.488	9 477	1.07	0.093	Α	3.648	3.640 1	1 00
	в	3.466	0.411			В	3.632		1.02
1.90	Α	3.556	2 559	1.04	.184	Α	3.752	3.710	1 00
	в	3.547	5.004			в	3.668		1.00
.283	А	3.604	3.604	1.03	.279	Α	3.829	3 779 0	0.08
	в	3.605				в	3.729	0.110	0.98
.376	Α	3.621	3.652	3.652 1.02	.367	Α	3.976	3 021	0.95
	в	3.683				в	3.871	0.021	0.00

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# Discussion of Results

The curves in Fig. 1 show how  $K_E$  increases with increasing salt concentration. Each salt has its own specific effect; and the salts sodium nitrite and sodium acetate *apparently* depress the equilibrium constant below the value 3.7. It is obvious, however, that in the case of sodium nitrite the reaction NaNO<sub>2</sub> + HAc  $\longrightarrow$  KAc + HNO<sub>2</sub> occurs; and our titration values really give the *total* acid present. We had evidence of the complications arising in the case of this salt in the fact that a considerable pressure developed and a number of filled tubes broke in heating. For this reason the results for this salt must be regarded merely as approximations to the true values.

The variation in  $K_E$  due to the presence of dissolved salts arises from the effects of these salts upon the activity coefficients of the reacting species in the equilibrium mixtures. The stoichiometrical concentrations are different in the final mixtures, but the ratio  $a_3a_4/a_1a_2$  is a constant always. Again, even though  $a_1, a_2, \ldots$  are not always the same in the final mixtures, the above ratio must always be constant, on account of the relation  $\overline{\mu}_1 + \overline{\mu}_2 = \overline{\mu}_3 + \overline{\mu}_4$ , which holds for chemical equilibrium, where  $\overline{\mu}$  is the mo-

lecular chemical potential. Any change in a potential of the lefthand member must be accompanied by a compensating change in the right-hand member. The relation between a, the activity, and C, the molar concentration, is given by a = fC; f varies with the nature of the thermodynamic environment.

Determination of Reaction Velocity Constants.—The velocity of the reaction  $C_2H_5OH + HAc$   $C_2H_5Ac + H_2O$  is given by the relation,  $V = k'f_1f_2C_1C_2 - k''f_3f_4C_3C_4$ , where f and C are the activity coefficient and molar concentration, respectively, at any instant, of a given species, and k' and k'' VI,  $NaC_2H_3O_2$ .



Fig. 1— $K_E$  values: I, NaBr mixtures; II, NaCl; III, NaCNS; IV, NaI; V, NaNO<sub>2</sub>; VI, NaC<sub>2</sub>H<sub>8</sub>O<sub>2</sub>.

are constants; f may be expressed as a function of  $\mu$ , the ionic strength,<sup>6</sup>  $\log f = \mu k$ , or  $f = e^{\mu k}$ . Hence, for V we can write

$$V = k' e^{\mu(k_1 + k_2)} C_1 C_2 - k'' e^{\mu(k_3 + k_4)} C_3 C_4$$

Unfortunately, we do not know the values of  $k_1$ ,  $k_2$ —, so that we are unable to use the above equation directly for the determination of k'and k''. We are forced, therefore, to use the classical expression for V, namely

$$V = k_1 C_1 C_2 - k_2 C_3 C_4$$

and to calculate  $k_1$  and  $k_2$  solely by an application of mathematics, and then to attempt a determination of the true values of k' and k''.

For the reaction  $C_2H_5OH + CH_3COOH \implies CH_3COOC_2H_5 + H_2O$ , let *a*, *b*, *c* and *d* denote the initial concentrations in moles per liter of alcohol, acid, ester and water, and let the amount of change after the time *t* be *x*. The velocities of the direct and reverse reactions are

$$\frac{dx_1}{dt} = k_1(a - x) (b - x), \ \frac{dx_2}{dt} = k_2 (c + x) (d + x)$$

hence the velocity of esterification is

$$\frac{dx}{dt} = k_1(a - x)(b - x) - k_2(c + x)(d + x)$$

This equation may be integrated, giving, finally, the expression

$$k_2 = \frac{1}{t} \cdot \frac{K-1}{P} \log \frac{(Q-P)[Q+P-2(K-1)x]}{(Q+P)[Q-P-2(K-1)x]}$$

where K is the equilibrium constant, defined by  $K = k_1/k_2$ 

$$P = \sqrt{Q^2 - 4(K - 1)(Kab - cd)}$$
 and  $Q = [K(a + b) + (c + d)]$ 

#### **Experimental Method**

The general procedure was similar to that described under the determination of  $K_E$ . Since the reaction rate is slow at room temperature, the actual starting time was not taken until the mixtures were sealed in tubes and the tubes immersed in boiling carbon tetrachloride. The time of stopping was taken when the tubes were withdrawn from the heating flask and immersed in ice water, prior to titration of the acetic acid present. Thus the time recorded in the tables represents the time during which the samples were at the temperature of boiling carbon tetrachloride.

The proportions of ethyl alcohol, acetic acid and salt solution in the initial mixture were the same as in the equilibrium experiments.

The values of  $k_2$  for the reaction were calculated from the data obtained by the use of the equation given above. For K in that equation we substituted the determined value  $K_E$  for the salt concentration used. However, the ratio  $k_1/k_2$  is probably not constant, so that the values given in Table V are the averages of the *last three measurements* only. In Table IV, however, we give complete values for two series, in order to show the trend of the values of  $k_2$ . We found this trend in all our series.

			Table I	V		
REACTION VI	LOCITY CO	NSTANTS IN P	RESENCE	of 0.200 N S	SODIUM CHLC	RIDE AND OF
		0.298 N Science 10.298	DDIUM T	HIOCYANATE		
0.2 N Sodium chloride Time, minutes $k_2$			Ti	0.3 N Sodium me, minutes	thiocyanate k2	
	73	0.000261		98	0.000181	
	138	.000228		137	.000119	
	198	.000222		174	.000116	
	230			263	.000113	
	288	.000215		297	.000105	
408		.000186		329	.000108	
			TABLE '	v		
THE EFFECT	OF VARIOU	s Salts upon $k_1 \cdot 10^4 =$	THE VI = $k_2$ .det	ELOCITY CONST 1. $K_E \cdot 10^4$	TANT $k_1$ (Ten	4p., 78°)
Salt concn.	NaCl	NaCNS	NaI	NaBr	NaAc	NaNO2
0.1	6.16	4.25	5.23	6.58	0.643	0.668
.2	8.46	4.43	5.75	8.39	.671	.529
.3	10.06	4.41	6.83	10.83	. 623	.753
.4	10.90	5.20	5.83	12.75	.623	.531
0.00 salt gave $k_1 \times 10^4 = 3.86$ . 0.02 HCl gave $k_1 \times 10^4 = 29.19$ .						

The results are shown graphically in Fig. 2.

# Discussion of Results

The effects of the anions in increasing the reaction velocity seem to be almost in the same order as that indicated in the displacement of equilibrium, except that here the iodide seems to have a greater effect than the thiocyanate ion.

The explanation of the cause of the increased velocities, that is, the catalytic effect, might be attempted in terms of various theories. These

theories may be summarized briefly as follows: (1) increased hydrogen-ion concentration,<sup>8</sup> (2)hydration of salt with resulting increase in hydrogen-ion concentration<sup>9</sup> (Manning's work,<sup>10</sup> however, seems to show that hydration of solute does not affect the reaction rate constants), (3) increased activity of hydrogen ion,<sup>11</sup> and of hydrogen ion and of the undissociated molecule, 12 (4) shift in the water equilibrium;13 this amounts to a change in solvent, in which concentrations, reaction velocities. ionization. etc., will be different from those in the original solvent, (5) the activity theory of reaction rate,14 (6) Brönsted's theory of reaction velocity,<sup>15</sup> (7) change in the thermodynamic potential caused



Fig. 2.—Reaction rate curves: I, NaBr mixtures; II, NaCl; III, NaI; IV, NaCNS; V, NaC<sub>2</sub>H<sub>8</sub>O<sub>2</sub>; VI, NaNO<sub>2</sub>.

by a change in the field surrounding the reacting substances.<sup>16</sup>

This last is substantially the hypothesis we have used in our investigation. We believe that the effect of salts upon equilibrium and velocity constants is due to changes in the activity coefficients of the reacting substances. This change itself is due to the new thermodynamic environment of the reacting substances in the presence of salts.

- <sup>8</sup> Arrhenius, Z. physik. Chem., 31, 197 (1899); Euler, ibid., 32, 348 (1900).
- <sup>9</sup> Wilson, This Journal, 42, 715 (1920).
- <sup>10</sup> Manning, J. Chem. Soc., 119, 2079 (1921).
- <sup>11</sup> Åkerlöf, Z. physik. Chem., 98, 260 (1921).
- <sup>12</sup> Taylor, This Journal, **37**, 551 (1915).
- <sup>13</sup> Bancroft, J. Phys. Chem., 30, 1194 (1926); Bowe, ibid., 31, 291 (1927).
- <sup>14</sup> Harned and Seltz, THIS JOURNAL, **44**, 1476 (1922).
- <sup>15</sup> Brönsted, Z. physik. Chem., **102**, 169 (1922).
- <sup>16</sup> Acree, This Journal, **41**, 474 (1919).

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Most other investigators of the influence of salts upon rates of esterification have used hydrochloric acid as well; and the increased velocity has been attributed to the increase in hydrogen-ion concentrations. Our investigations were carried out in the absence of mineral acid, so that if the presence of salts varied the hydrogen-ion concentration or activity, it was the hydrogen-ion concentration or activity resulting from the reaction mixture—acetic acid, ethyl alcohol and water.

Using our determined values for  $k_1$  and  $k_2$ , we may write

$$V = k_1 C_A C_B - k_2 C_E C_F \tag{1}$$

and also we may write

 $V = k'C_A C_B f_A f_B - k'' C_E C_F f_E f_F$ 

Then equating coefficients of like terms, we have

$$k_1 = k' f_A f_B; \quad k_2 = k'' f_E f_F \text{ or}$$
$$\log k_1 = \log k' + \log f_A + \log f_B, \text{ etc.}$$

If we assume that the Debye-McAuley relation holds for this system,

we have



Fig. 3.—I, NaBr mixtures; II, NaCl; III, NaI; IV, NaCNS; V, NaC<sub>2</sub>H<sub>3</sub>O<sub>2</sub>; VI, NaNO<sub>2</sub>.

Extrapolation to zero concentration of added salt gave the following values

For sodium bromide, 0.000537 For sodium chloride, 0.000457 For sodium iodide, 0.000467 For sodium thiocyanate, 0.000437

These values are somewhat higher than the value 0.000386 obtained for k' in the absence of salts.

We hope to continue the investigation in the region 0.10 to zero ionic strength of the four salts mentioned above, and also to extend the study

 $\log k_1 = \log k' + m\mu$ where *m* is a constant

 $\log k_1 = \log k' + \mu k_A + \mu k_B$ 

where m is a constant. We may test this relation by

plotting log  $k_1 + 5$  against  $\mu$ , which is here equal to C, the molar salt concentration. Such a plot is given in Fig. 3. Omitting entirely the plot for sodium nitrite, it is seen that the points fall approximately upon straight lines. While the points for sodium acetate fall very well upon a straight line, vet this line does not tend toward the same log  $k_1$  value for zero concentration as do the others. It is evident that a secondary salt effect has come into play in this case.

to salts of higher valence type. At the same time we are planning a study of the effect of the six salts upon the activity of the hydrogen ion of water and of acetic acid.

# Summary

The relation between the true equilibrium constant,  $K_a$ , for the ethyl acetate equilibrium in the presence of salts, and the constant  $K_E$  calculated from the classical mass action expression is  $K_a = K_E \Sigma f_1$ , where f is the activation of a given reacting species. The term  $\Sigma f$  varies with the salt present, giving rise to different values of  $K_E$ .

The value of  $K_E$  has been determined in the presence of the salts sodium bromide, sodium acetate and sodium nitrite. The values for sodium nitrite as added salt are considered to be only approximate. The value of  $K_E$  increases with the concentration of added salt. With sodium acetate as added salt,  $K_E$  is less than the value obtained in the absence of salts, and  $K_E$  increases linearly with the concentration of sodium acetate.

The velocity constants for the reaction have been determined by means of an expression which contains  $K_E$ , the determined equilibrium constant for the specific salt, and specific concentration. Values are reported for the specific reaction rates for the forward action for six salts. The values reported are those in the neighborhood of equilibrium where  $K_E = k_1/k_2$ .

The order of the effects of the salts upon the velocity of reaction is almost the same as that indicated in the displacement of equilibrium. The specific reaction rate is practically constant for all concentrations of sodium acetate. A secondary salt effect evidently occurs with sodium acetate, so that its effect cannot be interpreted in the same way as can the effects of the salts sodium iodide, bromide, chloride and thiocyanate.

The Debye-McAuley relation for the activity of non-electrolytes has been used to obtain an equation for the rate of the esterification reaction. This equation has been combined with the classical expression to obtain a relation to test the validity of the former equation. It has been shown that this equation is in substantial agreement with the experimental data.

Cincinnati, Ohio